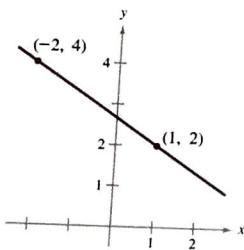


11.  $m = -\frac{2}{3}$

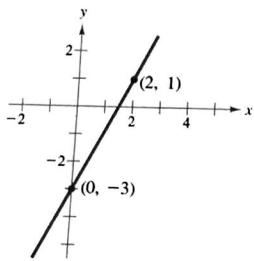


13.  $(0, 1), (1, 1), (3, 1)$

15.  $(0, 10), (2, 4), (3, 1)$

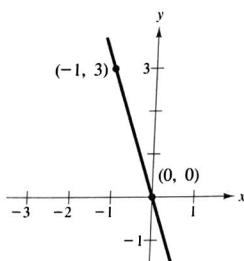
19.  $m$  is undefined, no  $y$ -intercept

21.  $2x - y - 3 = 0$

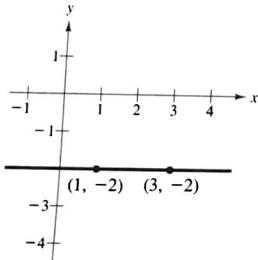


17.  $m = -\frac{1}{5}, (0, 4)$

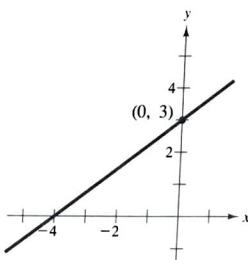
23.  $3x + y = 0$



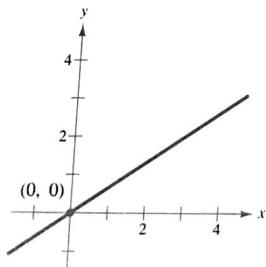
25.  $y + 2 = 0$



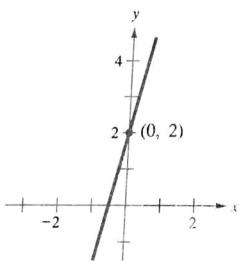
27.  $3x - 4y + 12 = 0$



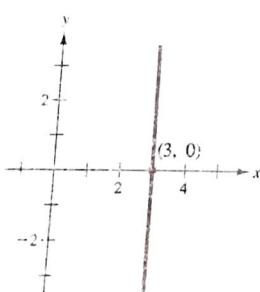
29.  $2x - 3y = 0$



31.  $4x - y + 2 = 0$

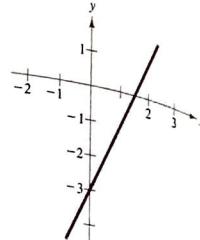
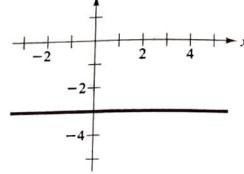


33.  $x - 3 = 0$

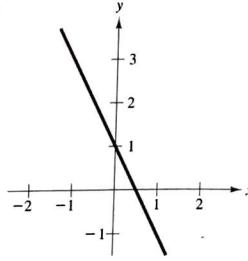


35.  $3x + 2y - 6 = 0$

37.  $12x + 3y + 2 = 0$   
 39.  $x + y - 3 = 0$   
 41. (a)  $2x - y - 3 = 0$       (b)  $x + 2y - 4 = 0$   
 43. (a)  $40x + 24y - 53 = 0$       (b)  $24x - 40y + 9 = 0$   
 45. (a)  $x - 2 = 0$       (b)  $y - 5 = 0$   
 47.  $49.$



51.



53.  $2x - y = 0$   
 55. Not collinear, because  $m_1 \neq m_2$   
 57.  $\left(0, \frac{-a^2 + b^2 + c^2}{2c}\right)$   
 59.  $\left(b, \frac{a^2 - b^2}{c}\right)$   
 61.  $5F - 9C - 160 = 0$   
 63.  $C = 0.25x + 95$   
 65.  $y = 875 - 175t$  where  $0 \leq t \leq 5$   
 67. (a)  $x = \frac{1}{15}(1130 - p)$       (b) 45 units  
 (c) 49 units  
 69. 2      71.  $\frac{5\sqrt{2}}{2}$       73.  $2\sqrt{2}$

## Section 1.5

3. (a)  $-3$       (b)  $-9$       (c)  $2b - 3$       (d)  $2x - 5$   
 5. (a)  $1$       (b)  $3$       (c)  $\sqrt{c + 3}$   
 (d)  $\sqrt{x + \Delta x + 3}$

5. (a) 1      (b) -1      (c) 1      (d)  $\frac{|x - 1|}{x - 1}$

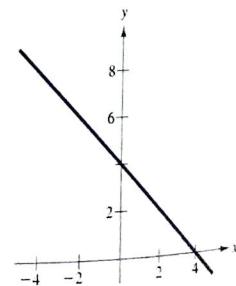
7.  $3 + \Delta x$       9.  $3x^2 + 3x\Delta x + (\Delta x)^2$

11.  $\frac{-1}{\sqrt{x - 1}(1 + \sqrt{x - 1})}$

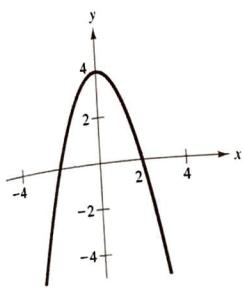
13.  $f(x) = 4 - x$

Domain:  $(-\infty, \infty)$

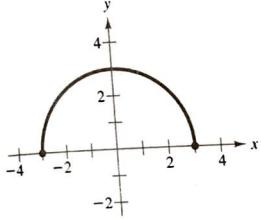
Range:  $(-\infty, \infty)$



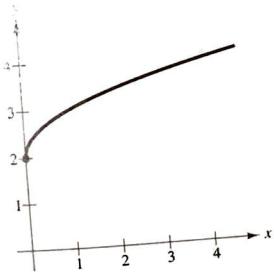
15.  $f(x) = 4 - x^2$   
Domain:  $(-\infty, \infty)$   
Range:  $(-\infty, 4]$



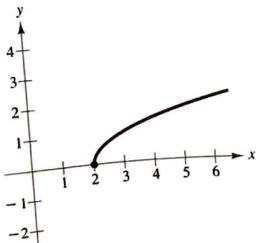
19.  $f(x) = \sqrt{9 - x^2}$   
Domain:  $[-3, 3]$   
Range:  $[0, 3]$



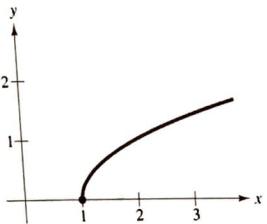
23.  $y$  is a function of  $x$   
27.  $y$  is a function of  $x$   
31.  $y$  is a function of  $x$   
35.  $y$  is not a function of  $x$   
37. (e)  $y = \sqrt{x} + 2$



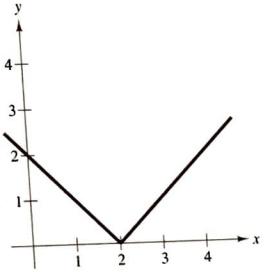
(c)  $y = \sqrt{x - 2}$



17.  $h(x) = \sqrt{x - 1}$   
Domain:  $[1, \infty)$   
Range:  $[0, \infty)$

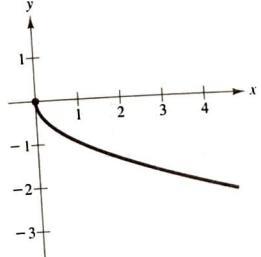


21.  $f(x) = |x - 2|$   
Domain:  $(-\infty, \infty)$   
Range:  $[0, \infty)$

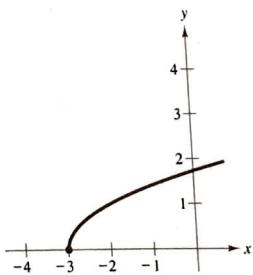


25.  $y$  is not a function of  $x$   
29.  $y$  is not a function of  $x$   
33.  $y$  is a function of  $x$

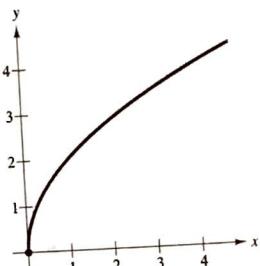
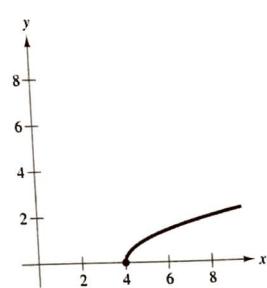
(b)  $y = -\sqrt{x}$



(d)  $y = \sqrt{x + 3}$



(e)  $y = \sqrt{x - 4}$   
(f)  $y = 2\sqrt{x}$



39. (a)  $y = (x + 3)^2$  (b)  $y = x^2 + 3$

41. (a) 0 (b) 0 (c) -1 (d)  $\sqrt{15}$

(e)  $\sqrt{x^2 - 1}$  (f)  $x - 1$

43.  $(f \circ g)(x) = x$

Domain:  $[0, \infty)$

$(g \circ f)(x) = |x|$

Domain:  $(-\infty, \infty)$

45.  $(f \circ g)(x) = \frac{x+1}{x}$

Domain:  $(-\infty, 0), (0, \infty)$

$(g \circ f)(x) = \frac{1}{x+1}$

Domain:  $(-\infty, -1), (-1, \infty)$

47.  $x = \pm 3$

49.  $\frac{10}{7}$

51. Even

53. Odd

55.  $R(x) = 4 - \frac{x^2}{2}, r(x) = 2$

57.  $h(x) = x^2, p(x) = x$

63.  $A = xy = x\left(\frac{100 - 2x}{2}\right) = x(50 - x)$

65.  $V = x(12 - 2x)^2$

67.  $V = 108x^2 - 4x^3$

69.  $T = \frac{\sqrt{x^2 + 4}}{2} + \frac{\sqrt{x^2 - 6x + 10}}{4}$

71.  $(A \circ r)(t) = 0.36\pi t^2$

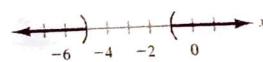
$A \circ r$  represents the area of the circle at time  $t$ .

## Review Exercises for Chapter 1

1.  $-1 \leq x \leq 5$



3.  $x < -5, x > -1$

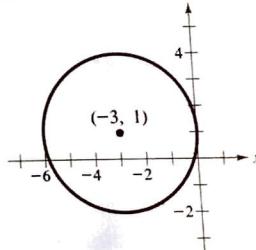


5.  $\frac{27}{16}$

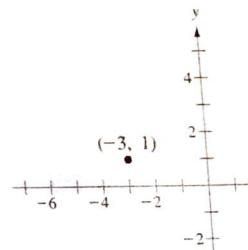
7.  $(-1, 3), (3, 2), (1, 1)$

9. Center:  $(-3, 1)$

Radius: 3

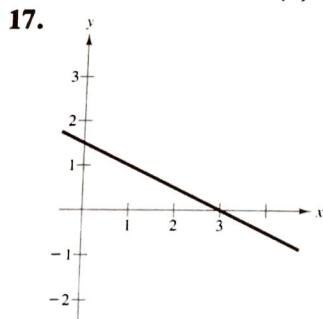


11. Point:  $(-3, 1)$

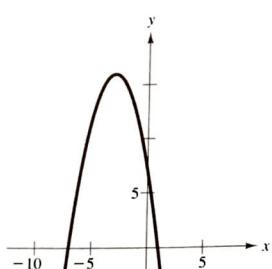


13.  $c = -21$     15.  $x^2 + y^2 - 2x - 4y - 4 = 0$

- (a) on the circle
- (b) inside the circle
- (c) outside the circle
- (d) inside the circle

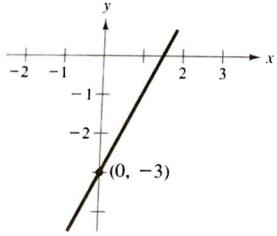


19.

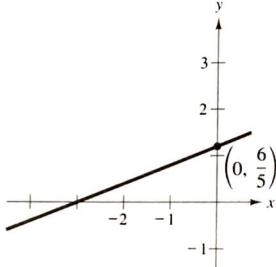


21. The points are not collinear.

23.



25.



27. (a)  $7x - 16y + 78 = 0$

(b)  $5x - 3y + 22 = 0$

(c)  $y + 2x = 0$

(d)  $x + 2 = 0$

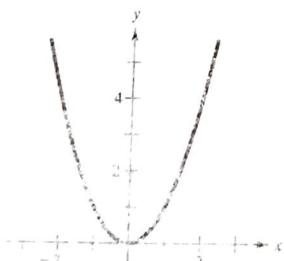
33.  $v = 850a + 300,000$

Domain:  $\{a: a \geq 0\}$

37.  $d = 45t$

Domain:  $\{t: t \geq 0\}$

41. Function

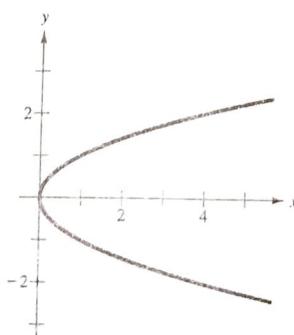


35.  $s = 6x^2$

Domain:  $\{x: x \geq 0\}$

39.  $P(x) = 500x - x^2$

43. Not a function



45. Function

47. (a)  $-x^2 + 2x + 2$

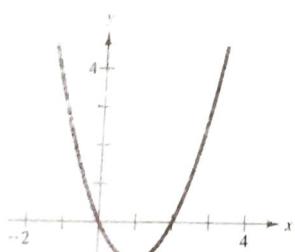
(b)  $-x^2 - 2x$

(c)  $-2x^3 - x^2 + 2x + 1$

(d)  $\frac{1-x^2}{2x+1}$

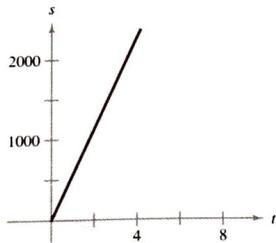
(e)  $-4x^2 - 4x$

(f)  $3 - 2x^2$



49. (a)

51.  $C = 0.30x + 150$



(b) Speed of the plane is 560 mi/hr

## Chapter 2

### Section 2.1

$x$	1.9	1.99	1.999
$f(x)$	0.3448	0.3344	0.3334

$x$	2.001	2.01	2.1
$f(x)$	0.3332	0.3322	0.3226

$$\lim_{x \rightarrow 2} \frac{x-2}{x^2 - x - 2} \approx 0.3333 \text{ (Actual limit is } \frac{1}{3} \text{.)}$$

$x$	-0.1	-0.01	-0.001
$f(x)$	0.2911	0.2889	0.2887

$x$	0.001	0.01	0.1
$f(x)$	0.2887	0.2884	0.2863

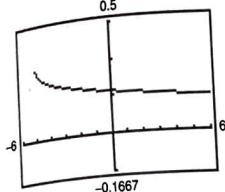
$$\lim_{x \rightarrow 0} \frac{\sqrt{x+3} - \sqrt{3}}{x} \approx 0.2887 \text{ (Actual limit is } \frac{1}{2\sqrt{3}} \text{.)}$$

$x$	2.9	2.99	2.999
$f(x)$	-0.0641	-0.0627	-0.0625

$x$	3.001	3.01	3.1
$f(x)$	-0.0625	-0.0623	-0.0610

$$\lim_{x \rightarrow 3} \frac{[1/(x+1)] - (1/4)}{x-3} \approx -0.0625$$

1. 1  
 3. 4  
 5.  $\frac{1}{2}$   
 7. (a) 15 (b) 5 (c) 6 (d)  $\frac{2}{3}$   
 9. 2  
 11. Limit does not exist.  
 13. -1  
 15. -2  
 17. -4  
 19. 2  
 21. 1  
 25. 2  
 27. (a) 64 (b) 2 (c) 12 (d) 8  
 29. (a)  $\lim_{x \rightarrow 4} f(x) = \frac{1}{6}$



n	$4 \pm [0.1]^n$	$f(4 \pm [0.1]^n)$
1	3.9000	6.9000
2	3.9900	6.9900
3	3.9990	6.9990
4	3.9999	6.9999
4	4.0001	7.0001
3	4.0010	7.0010
2	4.0100	7.0100
1	4.1000	7.1000

35. If  $\lim_{x \rightarrow 2} f(x) = 4$ , we cannot conclude anything about  $f(2)$ .  $f(2)$  may not exist at all, or  $f(2)$  may be some value other than 4.

## Section 2.2

1. (a) 1 (b) 3  
 7.  $\frac{1}{6}$   
 9. 12  
 11. 2  
 13.  $2x - 2$   
 15.  $\frac{1}{10}$   
 17.  $\frac{3}{2}$   
 19.  $\frac{\sqrt{3}}{6}$   
 21.  $-\frac{1}{4}$

x	-0.1	-0.01	-0.001
f(x)	0.358	0.354	0.354

x	0.001	0.01	0.1
f(x)	0.354	0.353	0.349

$$\lim_{x \rightarrow 0} \frac{\sqrt{x+2} - \sqrt{2}}{x} \approx 0.354 \quad (\text{Actual limit is } \frac{1}{2\sqrt{2}}.)$$

x	-0.1	-0.01	-0.001
f(x)	-0.263	-0.251	-0.250

x	0.001	0.01	0.1
f(x)	-0.250	-0.249	-0.238

$$\lim_{x \rightarrow 0} \frac{[1/(2+x)] - (1/2)}{x} \approx -0.250$$

(Actual limit is  $-\frac{1}{4}$ .)

27. (a) 1 (b) 1 (c) 1  
 29. (a) 0 (b) 0 (c) 0

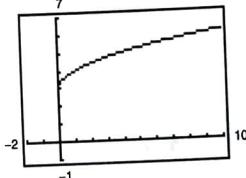
31. (a) 3 (b) -3 (c) Limit does not exist.  
 33.  $\frac{1}{10}$  35. Limit does not exist. 37. 2

39.  $-\frac{1}{x^2}$  41. Limit does not exist.

43. Limit does not exist. 45. 2 47. -2

49. 1 51. -16 ft/sec

53.



Domain:  $\{x: 0 \leq x < 9, x > 9\}$

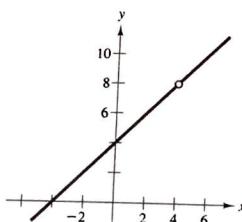
$$\lim_{x \rightarrow 9} f(x) = 6$$

It is not obvious from the graph that the function does not exist at  $x = 9$ .

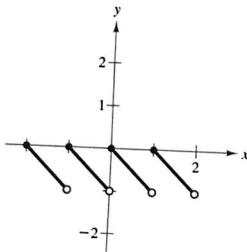
## Section 2.3

1. Continuous for all real  $x$
3. Discontinuous at  $x = -1$
5. Discontinuous at  $x = 1$
7. Continuous for all real  $x$
9. Nonremovable discontinuity at  $x = 1$
11. Continuous for all real  $x$
13. Removable discontinuity at  $x = -2$ ; nonremovable discontinuity at  $x = 5$
15. Continuous for all real  $x$
17. Nonremovable discontinuity at  $x = 2$
19. Nonremovable discontinuity at  $x = -2$
21. Continuous for all real  $x$
23. Nonremovable discontinuities at each integer
25. Continuous for all real  $x$
27. Continuous for all real  $x$
29. Removable discontinuity at  $x = 1$

**31.** Removable discontinuity at  $x = 4$



**33.** Nonremovable discontinuity at each integer



**35.**  $(-\infty, -6), (-6, 6), (6, \infty)$     **37.**  $(-\infty, \infty)$

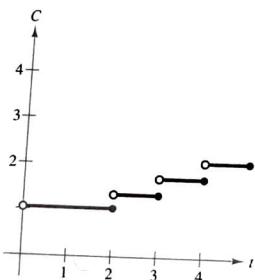
**41.** (a)  $(0.6, 0.7)$     (b)  $(0.68, 0.69)$

**43.**  $f(3) = 11$     **45.**  $f(2) = 4$     **47.**  $a = 2$

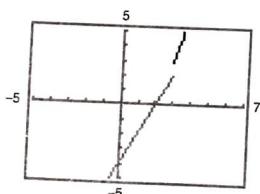
**49.** Yes,  $f$  is continuous on  $[-1, 1]$ .

$$\begin{aligned} \text{51. } C = & \begin{cases} 1.04, & 0 < t \leq 2 \\ 1.04 + 0.36[t - 1], & t > 2, t \text{ is not an integer} \\ 1.04 + 0.36(t - 1), & t > 2, t \text{ is an integer} \end{cases} \end{aligned}$$

Nonremovable discontinuity at each integer greater than 2



**53.** Discontinuous at  $x = 3$



## Section 2.4

$$\text{1. } \lim_{x \rightarrow -2^+} \frac{1}{(x + 2)^2} = \infty \quad \lim_{x \rightarrow -2^-} \frac{1}{(x + 2)^2} = \infty$$

$$\text{3. } \lim_{x \rightarrow -3^+} \frac{1}{x^2 - 9} = -\infty \quad \lim_{x \rightarrow -3^-} \frac{1}{x^2 - 9} = \infty$$

$$\text{5. } \lim_{x \rightarrow -3^+} \frac{x^3}{x^2 - 9} = \infty \quad \lim_{x \rightarrow -3^-} \frac{x^3}{x^2 - 9} = -\infty$$

$$\text{7. } x = -1, x = 2 \quad \text{9. } x = 0$$

$$\text{11. } x = -2, x = 1 \quad \text{13. } x = \pm 2 \quad \text{15. } x = 0$$

$$\text{17. } x = -2, x = 1$$

**19.** Removable discontinuity at  $x = -1$

**21.** Vertical asymptote at  $x = -1$     **23.**  $-\infty$

**25.**  $\infty$     **27.**  $-\infty$     **29.**  $\frac{1}{2}$     **31.**  $\infty$     **33.**  $\infty$

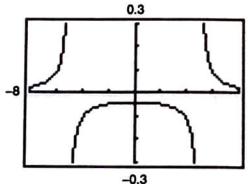
**35.**  $\infty$     **37.**  $-\infty$

**39.** (a) \$14,117.65    (b) \$80,000

(c) \$720,000    (d)  $\infty$

**41.** (a)  $\frac{7}{12}$  ft/sec    (b)  $\frac{3}{2}$  ft/sec    (c)  $\infty$

**43.**  $-\infty$



## Section 2.5

$$\text{1. } \lim_{x \rightarrow 2} (3x + 2) = 8 \quad \text{Let } \delta = \frac{0.01}{3} \approx 0.0033.$$

$$\text{3. } \lim_{x \rightarrow 2} (x^2 - 3) = 1$$

Assume  $1 < x < 3$  and let  $\delta = \frac{0.01}{5} = 0.002$ .

$$\text{5. } \lim_{x \rightarrow 2} \frac{x^2 - 3x + 2}{x - 2} = 1 \quad \text{Let } \delta = 0.01.$$

$$\text{7. } \lim_{x \rightarrow 2} (x + 3) = 5 \quad \text{Let } \delta = \varepsilon.$$

$$\text{9. } \lim_{x \rightarrow 6} 3 = 3 \quad \text{Any } \delta \text{ will work.}$$

$$\text{11. } \lim_{x \rightarrow 0} \sqrt[3]{x} = 0 \quad \text{Let } \delta = \varepsilon^3.$$

$$\text{13. } \lim_{x \rightarrow 0} x^2 = 0 \quad \text{Let } \delta = \sqrt{\varepsilon}.$$

$$\text{15. } \lim_{x \rightarrow 2} \frac{x^2 + x - 6}{x - 2} = 5 \quad \text{Let } \delta = \varepsilon.$$

$$\text{17. } \lim_{x \rightarrow 2} \frac{1}{x} = \frac{1}{2} \quad \text{Let } \delta = 2\varepsilon.$$

$$\text{19. } \lim_{x \rightarrow 2} (x^2 - 2) = 2 \quad \text{Let } \delta = \frac{\varepsilon}{5}.$$

$$\text{21. } \lim_{x \rightarrow 0^+} \sqrt{x} = 0 \quad \text{Let } \delta = \varepsilon^2.$$

$$\text{23. } \lim_{x \rightarrow -1^+} \frac{1}{x + 1} = \infty \quad \text{Let } \delta = \frac{1}{M}.$$

$$\text{25. } \lim_{x \rightarrow 2} \frac{1}{(x - 2)^2} = \infty \quad \text{Let } \delta = \frac{1}{\sqrt{M}}.$$

$$\text{27. } \lim_{x \rightarrow 3} x^2 = f(3) = 9 \quad \text{29. } 4$$

## Review Exercises for Chapter 2

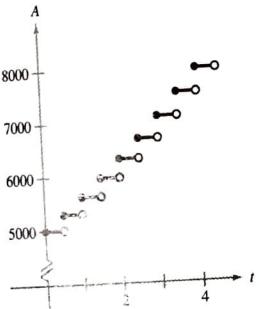
1. 7    3.  $\frac{77}{-\infty}$     5.  $\frac{10}{3}$     7.  $-\frac{1}{4}$     9.  $-1$   
 11. 3    13.  $-\infty$     15.  $-\infty$     17.  $\frac{1}{3}$     19. 0

21.	$x$	1.1	1.01	1.001	1.0001
	$f(x)$	0.5680	0.5764	0.5773	0.5773

$$\lim_{x \rightarrow 1^+} \frac{\sqrt{2x+1} - \sqrt{3}}{x-1} \approx 0.577$$

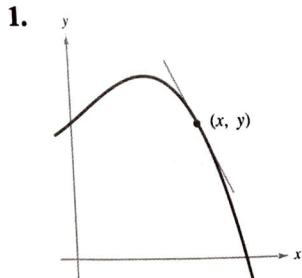
23.  $\frac{1}{\sqrt{3}}$     25. False    27. False    29. True

31. Nonremovable discontinuity at each integer  
 33. Removable discontinuity at  $x = 1$   
 35. Nonremovable discontinuity at  $x = 2$   
 37. Nonremovable discontinuity at  $x = -1$   
 39.  $c = -\frac{1}{2}$   
 41. Nonremovable discontinuity every 6 months



## Chapter 3

## Section 3.1

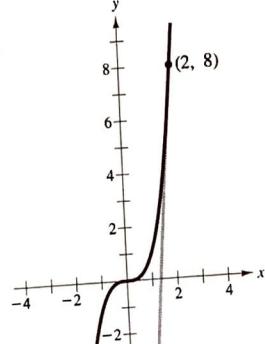
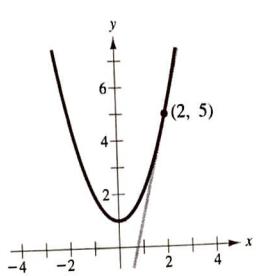


3. (a)  $m = 0$   
 (b)  $m = -3$

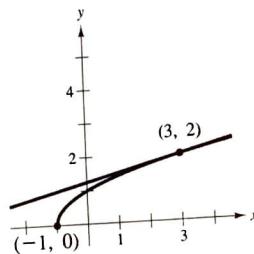
5.  $f'(x) = 0$     7.  $f'(x) = -5$   
 9.  $f'(x) = 4x + 1$     11.  $f'(x) = -\frac{1}{(x-1)^2}$   
 13.  $f'(t) = 3t^2 - 12$

15.  $f'(x) = 2x$   
 Tangent line:  
 $y = 4x - 3$

17.  $f'(x) = 3x^2$   
 Tangent line:  
 $y = 12x - 16$



19.  $f'(x) = \frac{1}{2\sqrt{x+1}}$   
 Tangent line:  $4y = x + 5$



$$21. f(x) = x^2 - 1$$

$$f'(2) = \lim_{x \rightarrow 2} \frac{f(x) - f(2)}{x - 2}$$

$$= \lim_{x \rightarrow 2} \frac{(x^2 - 1) - 3}{x - 2}$$

$$= \lim_{x \rightarrow 2} (x + 2) = 4$$

$$23. f(x) = x^3 + 2x^2 + 1$$

$$f'(-2) = \lim_{x \rightarrow -2} \frac{f(x) - f(-2)}{x + 2}$$

$$= \lim_{x \rightarrow -2} \frac{(x^3 + 2x^2 + 1) - 1}{x + 2}$$

$$= \lim_{x \rightarrow -2} x^2 = 4$$

$$25. f(x) = (x-1)^{2/3}$$

$$f'(1) = \lim_{x \rightarrow 1} \frac{f(x) - f(1)}{x - 1}$$

$$= \lim_{x \rightarrow 1} \frac{(x-1)^{2/3} - 0}{x - 1}$$

$$= \lim_{x \rightarrow 1} \frac{1}{(x-1)^{1/3}}$$

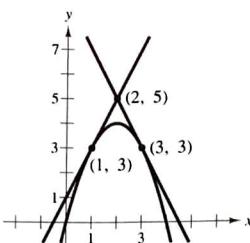
Limit does not exist.

$f$  is not differentiable at  $x = 1$ .

27.  $(-\infty, -3), (-3, \infty)$     29.  $(-\infty, -1), (-1, \infty)$   
 31.  $(-\infty, 3), (3, \infty)$     33.  $(1, \infty)$   
 35.  $(-\infty, 0), (0, \infty)$     37. (a) 3    (b) -3  
 39.  $f$  is not differentiable at  $x = 1$ .    41.  $f'(1) = 0$

43.  $y = 3x - 2$   
 $y = 3x + 2$

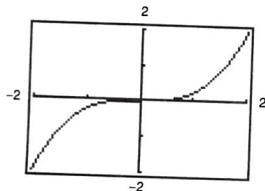
45.  $y = 2x + 1$   
 $y = -2x + 9$



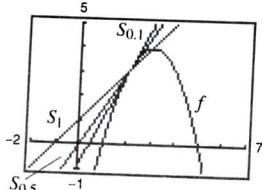
47. True    49. True

51.	$x$	-2	-1.5	-1	-0.5
	$f(x)$	-2	-0.84375	-0.25	-0.03125
	$f'(x)$	3	1.6875	0.75	0.1875

	$x$	0	0.5	1	1.5	2
	$f(x)$	0	0.03125	0.25	0.84375	2
	$f'(x)$	0	0.1875	0.75	1.6875	3



53. (a)



(b) The graphs of  $S$  for decreasing values of  $\Delta x$  are secant lines approaching the tangent line to the graph of  $f$  at the point  $(2, f(2))$ .

## Section 3.2

1. Average rate: 2  
 Instantaneous rates:  
 $f'(1) = 2$   
 $f'(2) = 2$

3. Average rate:  $-\frac{1}{4}$   
 Instantaneous rates:  
 $f'(0) = -1$   
 $f'(3) = -\frac{1}{16}$

5. Average rate: 4.1  
 Instantaneous rates:  
 $f'(2) = 4$   
 $f'(2.1) = 4.2$

7. (a) -48 ft/sec  
 (b)  $s'(1) = -32$  ft/sec  
 $s'(2) = -64$  ft/sec  
 (c)  $t = \frac{15\sqrt{6}}{4} \approx 9.2$  sec  
 (d) -293.9 ft/sec

9.  $v(5) = 224$  ft/sec,  $v(10) = 64$  ft/sec

11.  $v\left(\frac{5\sqrt{6}}{2}\right) = -80\sqrt{6}$  ft/sec  $\approx -195.96$  ft/sec

13. 740 ft

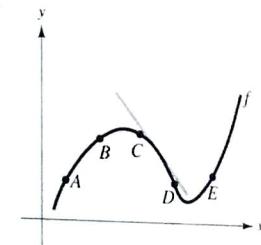
15.

17.

19.  $2x$     21.  $\frac{2}{x^2}$     23. 0    25.  $-\$1.91, -\$1.93$

27. (a) 50    (b) 33.33

29.  $\frac{dT}{dt} = K(T - T_a)$     31. (a) A and B  
 (b) Greater  
 (c)



(d) B and C, D and E

## Section 3.3

1. (a)  $\frac{1}{2}$     5. 1    7.  $2x$     9.  $-4t + 3$     11.  $3t^2 - 2$

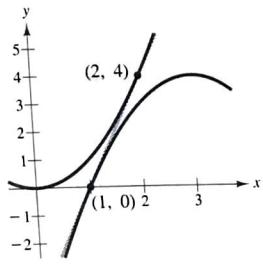
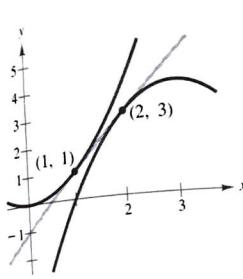
13. -1    15. 0    17. 4    19.  $2x + \frac{4}{x^2}$

21.  $3x^2 - 3 + \frac{8}{x^5}$     23.  $\frac{x^3 - 8}{x^3}$     25.  $3x^2 + 1$

27.  $\frac{4}{5x^{1/5}}$     29.  $\frac{1}{3x^{2/3}} + \frac{1}{5x^{4/5}}$

Function	Rewrite	Derivative	Simplify
31. $y = \frac{1}{3x^3}$	$y = \frac{1}{3}x^{-3}$	$y' = -x^{-4}$	$y' = -\frac{1}{x^4}$
33. $y = \frac{1}{(3x)^3}$	$y = \frac{1}{27}x^{-3}$	$y' = -\frac{1}{9}x^{-4}$	$y' = -\frac{1}{9x^4}$
35. $y = \frac{\sqrt{x}}{x}$	$y = x^{-1/2}$	$y' = -\frac{1}{2}x^{-3/2}$	$y' = -\frac{1}{2x^{3/2}}$

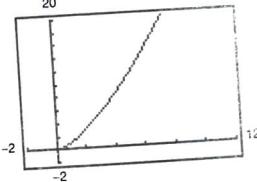
37.  $2x + y - 2 = 0$   
 39.  $(0, 2), \left(\sqrt{\frac{3}{2}}, -\frac{1}{4}\right), \left(-\sqrt{\frac{3}{2}}, -\frac{1}{4}\right)$   
 41. No horizontal tangents  
 43.  $y = 2x - 1$



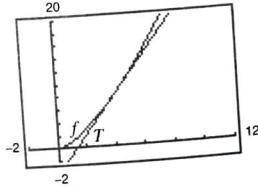
45. 8  
 47. (a) 10,000 (b) 4000 (c) 0 (d) -8000  
 49. (a)  $\frac{4}{9}$  (b)  $\frac{1}{3}$  (c) 0 (d)  $-\frac{5}{9}$   
 51. -44.1 ft/sec

53. -5.4 ft/sec<sup>2</sup>  
Approximately  $\frac{1}{6}$  the acceleration due to gravity on earth.

55. True  
57. (a)



(b)  $T(x) = 3(x - 4) + 8 = 3x - 4$



It becomes less accurate.

$\Delta x$	-2	-0.5	-0.1
$f(4 + \Delta x)$	2.828	6.458	7.702
$T(4 + \Delta x)$	2	6.5	7.7

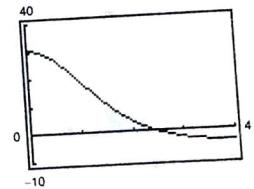
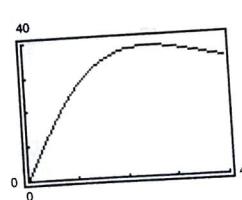
$\Delta x$	0	0.1	0.5	2
$f(4 + \Delta x)$	8	8.302	9.456	14.697
$T(4 + \Delta x)$	8	8.3	9.5	14

## Section 3.4

1.  $f'(x) = 2x^2, f'(0) = 0$   
 3.  $f'(x) = 5[x^{-2}(1) + (x + 3)(-2x^{-3})]$   
 $= -\frac{5(x + 6)}{x^3}$   
 $f'(1) = -35$   
 5.  $f'(x) = (x^3 - 3x)(4x + 3) + (2x^2 + 3x + 5)(3x^2 - 3)$   
 $= 10x^4 + 12x^3 - 3x^2 - 18x - 15$   
 $f'(0) = -15$   
 7.  $f'(x) = (x^5 - 3x)\left(-\frac{2}{x^3}\right) + \left(\frac{1}{x^2}\right)(5x^4 - 3)$   
 $= 3x^2 + \frac{3}{x^2}$

9.  $\frac{(2x - 3)(3) - (3x - 2)(2)}{(2x - 3)^2} = -\frac{5}{(2x - 3)^2}$   
 11.  $\frac{(x^2 - 1)(-2 - 2x) - (3 - 2x - x^2)(2x)}{(x^2 - 1)^2} = \frac{2}{(x + 1)^2}$   
 13.  $\frac{\sqrt{x}(1) - (x + 1)[1/(2\sqrt{x})]}{x} = \frac{x - 1}{2x^{3/2}}$   
 15.  $\frac{(t^2 + 2t + 2)(1) - (t + 1)(2t + 2)}{(t^2 + 2t + 2)^2} = \frac{-t^2 - 2t}{(t^2 + 2t + 2)^2}$   
 17.  $6s^2(s^3 - 2)$   
 19.  $\left(\frac{x+1}{x+2}\right)(2) + (2x-5)\left[\frac{(x+2)(1) - (x+1)(1)}{(x+2)^2}\right]$   
 $= \frac{2x^2 + 8x - 1}{(x+2)^2}$   
 21.  $15x^4 - 48x^3 - 33x^2 - 32x - 20$   
 23.  $\frac{(c^2 + x^2)(-2x) - (c^2 - x^2)(2x)}{(c^2 + x^2)^2} = -\frac{4xc^2}{(c^2 + x^2)^2}$

Function	Rewrite	Derivative	Simplify
25. $y = \frac{x^2 + 2x}{x}$	$y = x + 2$	$y' = 1$	$y' = 1$
27. $y = \frac{7}{3x^3}$	$y = \frac{7}{3}x^{-3}$	$y' = -7x^{-4}$	$y' = -\frac{7}{x^4}$
29. $y = \frac{3x^2 - 5}{7}$	$y = \frac{1}{7}(3x^2 - 5)$	$y' = \frac{1}{7}(6x)$	$y' = \frac{6x}{7}$
31. $\frac{3}{\sqrt{x}}$	33. $\frac{2}{(x-1)^3}$	35. $y = -x + 4$	
37. $y = -x - 2$	39. $(0, 0), (2, 4)$		
41. (a) -0.48	(b) 0.12	(c) 0.0149	43. 31.55
45. $a(2) = 4.069$			



**Section 3.5**

$$y = f(g(x))$$

$$1. y = (6x - 5)^4$$

$$3. y = \sqrt{x^2 - 1}$$

$$5. y = (x^2 - 3x + 4)^6$$

$$7. 6(2x - 7)^2$$

$$9. 12(9x - 4)^3(9) = 108(9x - 4)^3$$

$$11. -\frac{1}{(x - 2)^2}$$

$$13. -2(t - 3)^{-3}(1) = -\frac{2}{(t - 3)^3}$$

$$15. -3(x^3 - 4)^{-2}(3x^2) = -\frac{9x^2}{(x^3 - 4)^2}$$

$$17. x^2[4(x - 2)^3(1)] + (x - 2)^4(2x) = 2x(x - 2)^3(3x - 2)$$

$$19. \frac{1}{2}(1 - t)^{-1/2}(-1) = -\frac{1}{2\sqrt{1 - t}}$$

$$21. \frac{1}{2}(t^2 + 2t - 1)^{-1/2}(2t + 2) = \frac{t + 1}{\sqrt{t^2 + 2t - 1}}$$

$$23. \frac{1}{3}(9x^2 + 4)^{-2/3}(18x) = \frac{6x}{(9x^2 + 4)^{2/3}}$$

$$25. (4 - x^2)^{-1/2}(-2x) = -\frac{2x}{\sqrt{4 - x^2}}$$

$$27. \frac{2}{3}(9 - x^2)^{-1/3}(-2x) = -\frac{4x}{3(9 - x^2)^{1/3}}$$

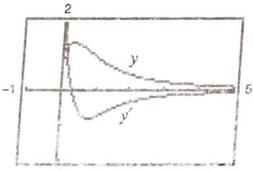
$$29. -\frac{1}{2(x + 2)^{3/2}}$$

$$31. x\left(\frac{1}{2}\right)(1 - x^2)^{-1/2}(-2x) + (1 - x^2)^{1/2}(1) = \frac{1 - 2x^2}{\sqrt{1 - x^2}}$$

$$33. \frac{(x^2 + 1)^{1/2}(1) - x(1/2)(x^2 + 1)^{-1/2}(2x)}{x^2 + 1} = \frac{1}{(x^2 + 1)^{3/2}}$$

$$35. \frac{(t - 1)(3) - (3t + 2)}{(t - 1)^2} = -\frac{5}{(t - 1)^2}$$

$$37. \frac{1 - 3x^2 - 4x^{3/2}}{2\sqrt{x}(x^2 + 1)^2}$$



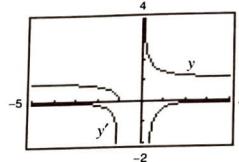
The zero of  $y'$  corresponds to the point on the graph of the function where the tangent line is horizontal.

$$39. \frac{3t(t^2 + 3t - 2)}{(t^2 + 2t - 1)^{3/2}}$$



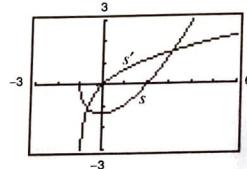
The zero of  $g'(x)$  corresponds to the point on the graph of the function where the tangent line is horizontal.

$$41. -\frac{\sqrt{\frac{x+1}{x}}}{2x(x+1)}$$



$y'$  has no zeros.

$$43. \frac{t}{\sqrt{1+t}}$$

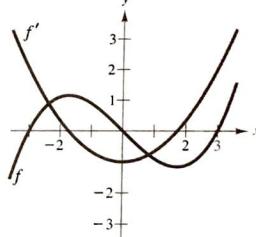


The zero of  $s'(t)$  corresponds to the point on the graph of the function where the tangent line is horizontal.

$$45. 9x - 5y - 2 = 0$$

$$49. \frac{3}{4(x^2 + x + 1)^{3/2}}$$

55.



The zeros of  $f'$  correspond to the points where the graph of  $f$  has horizontal tangents.

$$57. (a) 1.461 \quad (b) -1.016$$

**Section 3.6**

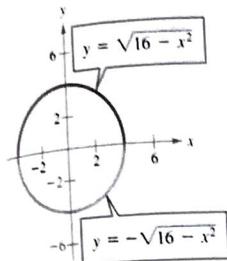
$$1. -\frac{x}{y}, -\frac{3\sqrt{7}}{7} \quad 3. -\frac{y}{x}, -\frac{1}{4} \quad 5. -\sqrt{\frac{y}{x}}, -\frac{5}{4}$$

$$7. \frac{y - 3x^2}{2y - x}, \frac{1}{2} \quad 9. \frac{18x}{(x^2 + 9)^2y}, \text{ undefined}$$

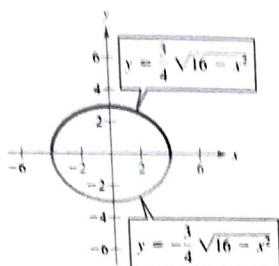
$$11. \frac{1 - 3x^2y^3}{3x^3y^2 - 1}, -1 \quad 13. -\sqrt[3]{\frac{y}{x}}, -\frac{1}{2}$$

$$15. \frac{4xy - 3x^2 - 3y^2}{2x(3y - x)}, -\frac{15}{28} \quad 17. -\frac{1}{2} \quad 19. 0$$

21.  $y' = -\frac{x}{y}$



23.  $y' = -\frac{9x}{16y}$



25.  $\frac{10}{x^3}$     27.  $-\frac{16}{y^3}$     29.  $\frac{3x}{4y}$

31. (a) At  $(4, 3)$ :

Tangent line:  $4x + 3y - 25 = 0$

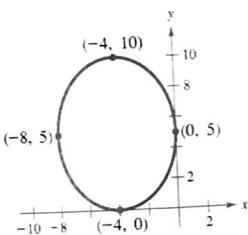
Normal line:  $3x - 4y = 0$

(b) At  $(-3, 4)$ :

Tangent line:  $3x - 4y + 25 = 0$

Normal line:  $4x + 3y = 0$

33. Horizontal tangents:  $(-4, 0), (-4, 10)$   
Vertical tangents:  $(0, 5), (-8, 5)$



35. At  $(1, 2)$ :

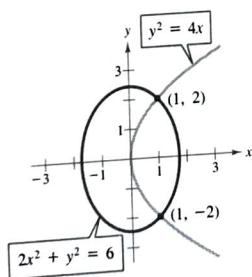
Slope of ellipse:  $-1$

Slope of parabola:  $1$

At  $(1, -2)$ :

Slope of ellipse:  $1$

Slope of parabola:  $-1$



37. At  $(\sqrt{2}, -\sqrt{2})$ :

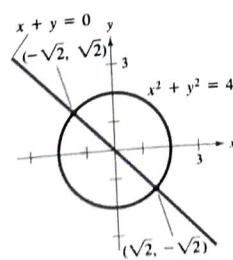
Slope of line:  $-1$

Slope of circle:  $1$

At  $(-\sqrt{2}, \sqrt{2})$ :

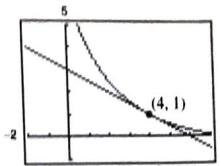
Slope of line:  $-1$

Slope of circle:  $1$



39.  $(x - 1 - 2\sqrt{2})^2 + (y - 2 + 2\sqrt{2})^2 = 16$   
 $(x - 1 + 2\sqrt{2})^2 + (y - 2 - 2\sqrt{2})^2 = 16$

41.  $x + 2y - 6 = 0$



## Section 3.7

1. (a)  $\frac{3}{4}$     (b) 20    3. (a)  $-\frac{5}{8}$     (b)  $\frac{3}{2}$

5. (a)  $24\pi$  in.<sup>2</sup>/min    (b)  $96\pi$  in.<sup>2</sup>/min

7. If  $dr/dt$  is constant,  $dA/dt$  is proportional to  $r$ .

9. (a)  $\frac{5}{\pi}$  ft/min    (b)  $\frac{5}{4\pi}$  ft/min

11.  $\frac{8}{405\pi}$  ft/min

13. (a) 9 cm<sup>3</sup>/sec    (b) 900 cm<sup>3</sup>/sec

15. (a) 0 cm/min    (b) 12 cm/min

17. (a)  $\frac{8}{25}$  cm/min    (b) 0 cm/min  
(c)  $-\frac{8}{25}$  cm/min    (d)  $-0.0039$  cm/min

19. (a) 24.6%    (b)  $\frac{1}{64}$  ft/min

21. (a)  $-\frac{7}{12}$  ft/sec    (b)  $-\frac{3}{2}$  ft/sec    (c)  $-\frac{48}{7}$  ft/sec

23. 21.96 ft<sup>2</sup>/sec

25. (a) 750 mi/hr    (b) 20 minutes

27.  $-\frac{28}{\sqrt{10}} \approx -8.85$  ft/sec

29. (a)  $\frac{25}{3}$  ft/sec    (b)  $\frac{10}{3}$  ft/sec

33.  $v^{0.3} \left( 1.3p \frac{dv}{dt} + v \frac{dp}{dt} \right) = 0$

## Review Exercises for Chapter 3

1.  $3x(x - 2)$     3.  $\frac{x + 1}{2x^{3/2}}$     5.  $-\frac{4}{3t^3}$

7.  $\frac{3x^2}{2\sqrt{x^3 + 1}}$     9.  $2(6x^3 - 9x^2 + 16x - 7)$

11.  $s(s^2 - 1)^{3/2}(8s^3 - 3s + 25)$     13.  $\frac{2x(2 - x)}{(x - 1)^2}$

15.  $-\frac{x^2 + 1}{(x^2 - 1)^2}$     17.  $32x - 128x^3$

19.  $\frac{6x}{(4 - 3x^2)^2}$     21.  $\frac{x + 2}{(x + 1)^{3/2}}$     23.  $\frac{5}{6(t + 1)^{1/6}}$

25.  $\frac{9}{(x^2 + 9)^{3/2}}$     27.  $\frac{2(t + 2)}{(1 - t)^4}$

29.  $\frac{2(6x^3 - 15x^2 - 18x + 5)}{(x^2 + 1)^3}$     31.  $-\frac{2x + 3y}{3(x + y^2)}$

33.  $\frac{2y\sqrt{x} - y\sqrt{y}}{2x\sqrt{y} - x\sqrt{x}}$     35.  $\frac{x}{y}$